

RAJ KUMAR GOEL INSTITUTE OF TECHNOLOGY & MANAGEMENT, GZB
1st Sessional Examination 2017-18 (Odd Semester)

Roll No.:

Year/Branch: 2nd Year CSE/IT

Max Time: 1 Hours 30 Minute

Subject Name: Discrete St. & Theory of Logic

Subject Code: RCS - 301

Max Marks: 50

SECTION-A

Q.1 Attempt all parts. Write answer of each part in short.

- (a) Prove that $(A \cup B)' = A' \cap B'$.
- (b) Show that $(p \vee q) \rightarrow r \equiv (p \rightarrow r) \wedge (q \rightarrow r)$.
- (c) Check whether relation $R = \{ (a,b) \mid a \geq b \}$ on set of real numbers is an equivalence relation or not.
- (d) Give the definition of recursively defined function
- (e) Give an example of a relation which is symmetric and transitive but not reflexive.

SECTION-B

Note: Attempt any five questions from this section.

- Q.2** Let R and S be the following relation on $A = \{ a, b, c, d \}$, defined
 $R = \{ (a, a), (a, c), (c, b), (c, d), (d, b) \}$ and $S = \{ (b, a), (c, c), (c, d), (d, a) \}$
Find (a) RoS (b) SoR (c) RoR (d) SoS
- Q.3** Analyse that $((p \vee q) \wedge \neg(\neg p \wedge (\neg q \vee \neg r))) \vee (\neg p \wedge \neg q) \vee (\neg p \wedge \neg r)$ is tautology.
- Q.4** Prove by mathematical induction $6 \text{pow}(n+2) + 7 \text{pow}(2n+1)$ is divisible by 43 for each positive integer n.
- Q.5** Let $R = \{ (1, 2), (2, 3), (3,1) \}$ and $A = \{ 1, 2, 3 \}$, find the reflexive, symmetric and transitive closure of R, using
- (i) Composition of relation R
(ii) Graphical representation of R
- Q.6** Define Identity Law, Idempotent Law, absorption and involution law of logic.
- Q.7** Write an equivalent formula for

$$p \wedge (q \leftrightarrow r) \vee (r \leftrightarrow p)$$

Which neither contains biconditional nor conditional connectives.

- Q.8** Let $A = \{ a,b,c \}$ and $R = \{ (a,a), (a,b), (a,c), (b,b), (c,c) \}$ then evaluate reflexive closure and symmetric closure.
- Q.9** Let $A = \{ 1, 2, 3, 4, 5, 6 \}$, construct pictorial description of relation R on A for the following:
- $R = \{ (J,K) : K \text{ is multiple of } J \}$
 - $R = \{ (J,K) : (J-K)^2 \in A \}$
 - $R = \{ (J,K) : J \text{ divides } K \}$
 - $R = \{ (J,K) : J \times K \text{ is prime} \}$

SECTION-C

Note: Attempt any two questions from this section.

- Q.10** Let R be a relation on N, the set of natural numbers such that
 $R = \{ (x, y) \mid 2x+3y \text{ and } x, y \in N \}$ Find
- (i) The domain and co-ordinate of R
(ii) R^{-1}
- Q.11** Let f, g and h be functions from N to N where N is set of natural numbers so that
 $f(x) = x + 1$, $g(x) = 2x$, $h(x) = \{ 0 \text{ if } x \text{ is even, } 1 \text{ if } x \text{ is odd} \}$. Determine
- (i) fof (ii) gof (iii) fog
(iv) goh (v) hog (vi) (fog)oh (vii) go(fog)oh
- Q.12** Use MI to show that $1 + 2 + 2^2 + \dots + 2^n = 2^{n+1} - 1$ for all non-negative integers n.